

## 1.7 Exploring Operations with Functions

<p><b>A Arithmetic Combinations</b> Consider two functions <math>f(x)</math> and <math>g(x)</math>. Then the sum <math>f + g</math>, difference <math>f - g</math>, product <math>fg</math> and the quotient <math>f / g</math> are defined as follows:</p> $(f + g)(x) = f(x) + g(x)$ $(f - g)(x) = f(x) - g(x)$ $(fg)(x) = f(x)g(x)$ $\left(\frac{f}{g}\right)(x) = \frac{f(x)}{g(x)}, \quad g(x) \neq 0$	<p>Ex 1. Given <math>f(x) = x^2 - 1</math> and <math>g(x) = 2\sqrt{x-1}</math>, find:</p> <p>a) <math>(f + g)(1)</math></p> <p>b) <math>(f - g)(2)</math></p> <p>c) <math>(fg)(5)</math></p> <p>d) <math>\left(\frac{f}{g}\right)(1)</math></p> <p>e) <math>(f + g)(x)</math></p> <p>f) <math>(f - g)(x)</math></p> <p>g) <math>(fg)(x)</math></p> <p>h) <math>\left(\frac{f}{g}\right)(x)</math></p>
<p><b>B Domain</b> The domain of <math>f + g</math>, <math>f - g</math>, and <math>fg</math> is <math>D_f \cap D_g</math> (the intersection between the domain of <math>f</math> and the domain of <math>g</math>).</p> <p>The domain of <math>\frac{f}{g}</math> is <math>\{x \in D_f \cap D_g \mid g(x) \neq 0\}</math>.</p>	<p>Ex 2. Given <math>f(x) = x^2 - 1</math> and <math>g(x) = \sqrt{x-2}</math>, find the domain of the following arithmetic combinations:</p> <p>a) <math>(f + g)(x)</math></p> <p>b) <math>(f - g)(x)</math></p> <p>c) <math>(fg)(x)</math></p> <p>d) <math>\left(\frac{f}{g}\right)(x)</math></p> <p>e) <math>\left(\frac{g}{f}\right)(x)</math></p>
<p>Ex 3. The function <math>f</math> has the x-intercepts <math>-1</math>, <math>1</math>, and <math>3</math> and the y-intercept is <math>4</math>. The function <math>g</math> has the x-intercepts <math>-2</math> and <math>-1</math> and the y-intercept is <math>1</math>. Find the x-intercepts and the y-intercept of the following arithmetic combinations:</p>	<p>a) <math>(fg)(x)</math></p> <p>b) <math>\left(\frac{f}{g}\right)(x)</math></p> <p>c) <math>\left(\frac{g}{f}\right)(x)</math></p>

**Reading:** Nelson Textbook, Pages 54-56

**Homework:** Nelson Textbook, Page 56: #1a, 2a, 3a, 4a, 7