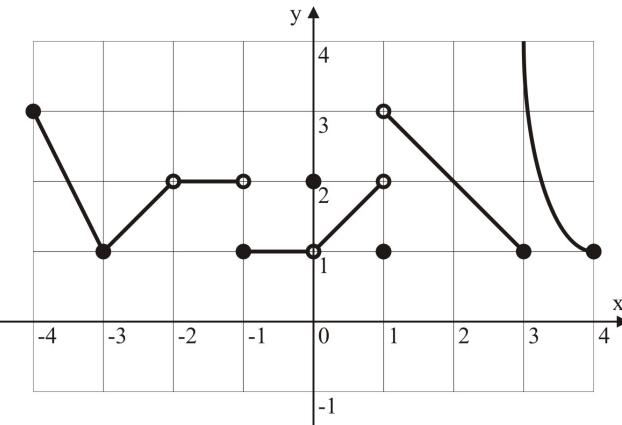


MCV4U Final Exam Review

Answer (or Solution)	Practice Questions
	<p>1. Consider the function $f(x)$ defined by the following graph:</p>
	<p>Find:</p> <p>a) $\lim_{x \rightarrow -2} f(x)$ b) $\lim_{x \rightarrow -1} f(x)$ c) $\lim_{x \rightarrow 1} f(x)$ d) $\lim_{x \rightarrow 3} f(x)$</p>
	<p>2. Evaluate the following limits.</p> <p>a) $\lim_{x \rightarrow 1} (x^3 - 2x^2 + 3x - 1)$ b) $\lim_{x \rightarrow 2} \frac{x+x^2}{x^3 - 2}$ c) $\lim_{x \rightarrow \pi/2} \sqrt{\sin x}$ d) $\lim_{x \rightarrow \pi} 2^{\cos x}$</p>
	<p>3. Consider the function:</p> $f(x) = \begin{cases} x+1 & \text{if } x < -1 \\ x^2 & \text{if } -1 \leq x \leq 1 \\ \sqrt{x} & \text{if } x > 1 \end{cases}$ <p>Find the following limits, if they exist.</p> <p>a) $\lim_{x \rightarrow -1} f(t)$ b) $\lim_{x \rightarrow 0} f(t)$ c) $\lim_{x \rightarrow 1} f(t)$</p>
	<p>4. Evaluate.</p> <p>a) $\lim_{x \rightarrow 2} \frac{x^2 - 4}{x + 2}$ b) $\lim_{x \rightarrow 1} \frac{x^2 + x - 2}{x - 1}$ c) $\lim_{x \rightarrow 2} \frac{x^3 - 8}{x^2 - 4}$ d) $\lim_{x \rightarrow 3} \frac{x^2 - 2x - 3}{x^2 - 4x + 3}$ e) $\lim_{x \rightarrow -3} \frac{x^3 + 27}{x + 3}$ f) $\lim_{x \rightarrow 2} \frac{\frac{1}{x} - \frac{1}{2}}{x - 2}$</p>
	<p>5. Evaluate.</p> <p>a) $\lim_{x \rightarrow 4} \frac{x - 4}{\sqrt{x} - 2}$ b) $\lim_{x \rightarrow 1} \frac{\sqrt{x} - x}{x - 1}$ c) $\lim_{x \rightarrow 2} \frac{\sqrt{6-x} - 2}{\sqrt{3-x} - 1}$ d) $\lim_{t \rightarrow 0} \frac{\sqrt{3+t} - \sqrt{3}}{t}$ e) $\lim_{x \rightarrow 1} \frac{\frac{1}{\sqrt{x}} - 1}{x - 1}$ f) $\lim_{t \rightarrow 0} \left(\frac{1}{t\sqrt{1+t}} - \frac{1}{t} \right)$</p>
	<p>6. Evaluate.</p> <p>a) $\lim_{x \rightarrow 8} \frac{x - 8}{\sqrt[3]{x} - 2}$ b) $\lim_{x \rightarrow 4} \frac{x^{3/2} - 8}{x - 4}$ c) $\lim_{x \rightarrow 1} \frac{\sqrt{x} - 1}{\sqrt[3]{x} - 1}$</p>

7. Consider the function $f(x)$ defined by the following graph:



For each value of $x = a$, classify the function $f(x)$ as continuous, having a jump, a removable or an infinite discontinuity.

- a) $a = -3$ b) $a = -1$ c) $a = 2$
 d) $a = 0$ e) $a = 3$

8. For what value of the constant c is the function

$$f(x) = \begin{cases} x + c & \text{if } x < 2 \\ cx^2 + 1 & \text{if } x \geq 2 \end{cases}$$

continuous at every number?

9. For each function, calculate first the slope of the tangent line with the formula:

$$m = \lim_{x \rightarrow a} \frac{f(x) - f(a)}{x - a}$$

then find the equation of the tangent line at the given point.

- a) $f(x) = x^2 + x$, at $P(-1, 0)$
 b) $f(x) = \frac{x-1}{x+1}$, at $P(1, 0)$

10. For each case find the slope of the tangent line at the general point $P(a, f(a))$ using $m = \lim_{h \rightarrow 0} \frac{f(a+h) - f(a)}{h}$.

- a) $f(x) = x^2$ b) $f(x) = x^3$
 c) $f(x) = x^2 - 2x + 1$ d) $f(x) = \frac{1}{x}$

11. For each case, find the ARC over the given interval.

- a) $f(x) = x^4 - x^3 + x^2$, $[-1, 1]$
 b) $f(x) = \frac{2x-1}{2x+1}$, $[0, 2]$

12. For each case, find the IRC at the given number.

- a) $f(x) = x^4 - x^3$, at $x = 1$
 b) $f(x) = \frac{x}{x^2 + 1}$, at $x = 0$

13. For each case, find the average velocity over the given interval.

- a) $s(t) = t^2 + t$, $[0, 2]$
 b) $s(t) = t^3 - t^2$, $[1, 2]$

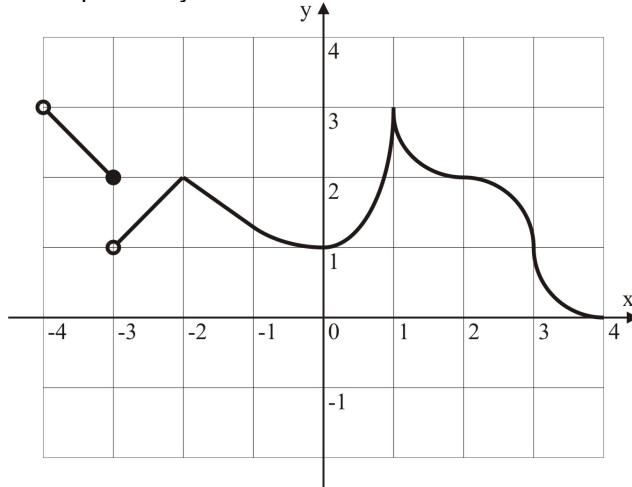
14. For each case, find the instantaneous velocity at the given moment of time.

- a) $s(t) = 2t^2 - t$, at $t = 1$
 b) $s(t) = 2t^3 - 3t$, at $t = 0$

1. Use the first principles method to find the derivative of each function. State the domain of each function and its derivative.

- a) $f(x) = 3$ b) $f(x) = -2x + 5$
c) $f(x) = 3x^2 - 2x + 1$ d) $f(x) = x^3 + 2x^2 + 3x + 4$
e) $f(x) = \sqrt{x}$

2. For the function $y = f(x)$ defined graphically below, find the values where the function f is not differentiable and explain why.



3. Use the power rule to differentiate.

- a) $f(x) = x$ b) $f(x) = x^2$ c) $f(x) = x^3$
d) $f(x) = x^0$ e) $f(x) = x^{-1}$ f) $f(x) = \frac{1}{x^2}$
g) $f(x) = \sqrt{x}$ h) $f(x) = \sqrt[3]{x}$ i) $f(x) = \sqrt{x^3}$

4. Differentiate.

- a) $f(x) = -3 \sin x$ b) $f(x) = 5 \cos x$
c) $f(x) = -4e^x$ d) $f(x) = -2 \ln x$

5. Differentiate.

- a) $f(x) = 1 - 2x + 3x^2$ b) $f(x) = x + \frac{2}{x} - \frac{3}{x^2} + x^3$
c) $f(x) = \sin x - \cos x$ d) $f(x) = -2e^x + 3 \ln x$

6. Find the equation of the tangent line to the curve $y = x^3 - 3x^2$ at the point $T(1, -2)$.

7. Find the equation of the tangent line(s) with the slope $m = -6$ to the curve $y = x^4 - 2x$.

8. At what points on the hyperbola $xy = 12$ is the tangent line parallel to the line $3x + y = 0$.

9. Differentiate.

- a) $f(x) = (x-1)(x+2)$ b) $f(x) = \sqrt{x}(\sqrt{x}-1)$
 c) $x \sin x$ d) xe^x e) $e^x \ln x$

10. Differentiate.

- a) $f(x) = (2x-1)^2$ b) $f(x) = (x-\sqrt{x})^2$
 c) $f(x) = (x^2 + x + 1)^{100}$
 d) $f(x) = \sin^3 x$ e) $f(x) = (\ln x)^5$

11. Differentiate, then simplify.

- a) $f(x) = \frac{x^2}{x-1}$ b) $f(x) = \frac{x^2-1}{x^2+1}$
 c) $f(x) = \frac{\sin x}{\cos x}$ d) $f(x) = \frac{\sin x}{e^x}$
 e) $f(x) = \frac{\sqrt{x}}{\ln x}$ f) $f(x) = \frac{\ln x}{\sin x}$

12. For each case, use $\frac{dy}{dx} = \frac{dy}{du} \frac{du}{dx}$ to find the derivative of $y = f(g(x))$.

- a) $y = u^5$, $u = 2x - 1$ b) $y = \sqrt{u}$, $u = x^2 + 1$

13. Use chain rule to differentiate.

- a) $y = [(x^2 - 1)^3 + x^2]^2$ b) $y = \frac{(1-x^2)^2}{(1-x)^3}$
 c) $y = \sqrt{x + \sqrt{x}}$

14. Use the generalized differentiation rules to find the derivative of each function.

- a) $y = (1+x+x^2)^{10}$ b) $y = \sqrt{x^2 - 2x}$
 c) $y = \sin \sqrt{x}$ d) $y = \sqrt{\cos x}$
 e) $y = \ln \sqrt{x}$ f) $y = \sqrt{x + e^x}$

15. For each case, find the first and the second derivative.

- a) $y = 1 - 3x + 4x^2$ b) $y = 4 - 2x + x^2 - 2x^3$
 c) $y = \frac{1}{x}$ d) $y = \frac{1}{x^2}$
 e) $y = \sqrt{x}$ f) $y = \frac{x}{x+1}$
 g) $y = \sin x$ h) $y = e^x$
 i) $y = \ln x$ j) $y = \log x$

16. For each case, find the velocity and the acceleration functions.

- a) $s(t) = 2t^2 - 3t + 1$ b) $s(t) = t^3 + 2t^2 + t - 3$
 c) $s(t) = \frac{t}{t+1}$

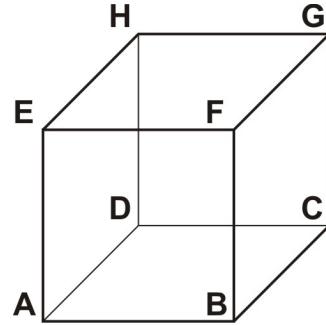
17. For each case, find the moments of time at which the object is at rest.

- a) $s(t) = t^3 - t$ b) $s(t) = 3t^4 - 6t^2$

	<p>1. For each case, use the first derivative sign to find the intervals of increase or decrease.</p> <p>a) $f(x) = x^2 - 2x$ b) $f(x) = \frac{x}{x-1}$ c) $f(x) = \frac{x}{x^2 + 1}$ d) $f(x) = \sqrt{x}(x-1)$</p> <p>2. Find the intervals of increase or decrease.</p> <p>a) $f(x) = x \ln x$ b) $f(x) = xe^x$ c) $f(x) = xe^{-x}$ d) $f(x) = x + \sin x$</p>
	<p>3. For each case, find the critical points.</p> <p>a) $f(x) = x^2 + 2x$ b) $f(x) = 2x^3 + 3x^2$ c) $f(x) = x$ d) $f(x) = \sqrt[3]{x}$ e) $f(x) = \frac{1}{x^2}$ f) $f(x) = \frac{x}{x^2 + 1}$</p> <p>4. For each case, find the critical points.</p> <p>a) $f(x) = \sin x$ b) $f(x) = \tan x$ c) $f(x) = e^x$ d) $f(x) = \ln x$ e) $f(x) = x \ln x$ f) $f(x) = xe^x$</p>
	<p>5. For each case, find any local extrema using the first derivative test.</p> <p>a) $f(x) = x^4 - 2x^2 + 1$ b) $f(x) = x^2(3 - 2x)$ c) $f(x) = \frac{1+x}{1-x}$ d) $f(x) = x - \sqrt{x}$ e) $f(x) = x^2 - \sqrt{x}$ f) $f(x) = x^2 - 4$</p>
	<p>6. For each case, find the absolute extrema (maximum or minimum) points.</p> <p>a) $f(x) = 2x^3 + 3x^2 - 12x + 1$, for $x \in [-3, 2]$ b) $f(x) = \frac{5x}{x+1}$, for $x \in [0, 4]$ c) $f(x) = x + \frac{4}{x}$, for $x \in [1, 4]$ d) $f(x) = \cos x$, for $x \in [-\pi/2, 2\pi]$ e) $f(x) = x \log x$, for $x \in [1, 10]$ f) $f(x) = xe^{-x}$, for $x \in [-1, 2]$ g) $f(x) = x + \sin x$, for $x \in [0, 2\pi]$</p>
	<p>7. For each case, find the intervals of concavity.</p> <p>a) $f(x) = x^4 - 6x^2$ b) $f(x) = (x^2 - 1)^3$ c) $f(x) = \frac{x}{x^2 - 1}$ d) $f(x) = (x-1)(x+1)^3$ e) $f(x) = x^2 e^x$ f) $f(x) = x \ln x$ g) $f(x) = x^2 \ln x$ h) $f(x) = x + \cos x$</p>

	<p>8. For each case, find the points of inflection.</p> <p>a) $f(x) = x^3 - x$ b) $f(x) = x + \frac{1}{x^2}$ c) $f(x) = (x+1)^{5/3}$ d) $f(x) = (1-x)^2(1+x)^2$ e) $f(x) = x^2 \ln x$ f) $f(x) = x - \sin x$</p> <p>9. Find c given that the graph of $f(x) = cx^2 + 1/x^2$ has a point of inflection at $(1, f(1))$.</p>
	<p>10. Use the second derivative test to find the local maximum and minimum values of each function.</p> <p>a) $f(x) = x^3 - 6x^2$ b) $f(x) = x^4 - 6x^2 - 5$ c) $f(x) = \frac{x}{x^2 + 1}$ d) $f(x) = \frac{x}{(x-1)^2}$</p> <p>11. Find the local minimum and maximum values for:</p> <p>a) $y = x^3$ b) $y = x^4$</p>
	<p>6. Second Derivative ⇒ compute $f''(x)$ ⇒ find points where $f''(x) = 0$ or $f''(x)$ DNE ⇒ find points of inflection ⇒ find intervals of concavity upward/downward ⇒ check the local extrema using the second derivative test</p> <p>7. Sketching ⇒ use broken lines to draw the asymptotes ⇒ plot x- and y- intercepts, extrema, and inflection points ⇒ draw the curve near the asymptotes ⇒ sketch the curve</p> <p>12. Sketch the graph of the following polynomial functions.</p> <p>a) $f(x) = 2x^3 - 3x^2 - 36x$ b) $f(x) = 3x^5 - 5x^3$ c) $f(x) = (x-1)^3$ d) $f(x) = x^2(x+3)$ e) $f(x) = (x^2 - 3)(x^2 - 5)$</p> <p>13. Sketch the graph of the following rational functions.</p> <p>a) $f(x) = \frac{x-1}{x+1}$ b) $f(x) = \frac{x}{x^2 - 1}$ c) $f(x) = \frac{x^2 + 1}{x^2 - 1}$ d) $f(x) = \frac{x^3}{x^2 + 1}$</p>
	<p>14. A rectangle has a perimeter of $100m$. What length and width should it have so that its area is a maximum. What is the maximum value of its area?</p> <p>15. If $2700cm^2$ of material is available to make a box with a square base and open top, find the dimensions of the box that give the largest volume of the box. What is the maximum value of the volume?</p> <p>16. A rectangular piece of paper with perimeter $100cm$ is to be rolled to form a cylindrical tube. Find the dimensions of the paper that will produce a tube with maximum volume.</p> <p>17. A farmer wants to fence an area of $240,000m^2$ in a rectangular field and divide it in half with a fence parallel to one of the sides of the rectangle. How can be done so as to minimize the cost of the fence?</p> <p>18. A metal cylinder container with an open top is to hold 1ft^3. If there is no waste in construction, find the dimensions that require the least amount of material.</p>

1. Consider the cube $ABCDEFGH$ with the side length equal to 10cm . Find the magnitude of the following vectors:
- \vec{AB}
 - \vec{BD}
 - \vec{BH}



2. Prove or disprove each statement.

- If $\vec{a} = \vec{b}$ then $|\vec{a}| = |\vec{b}|$.
- If $|\vec{a}| = |\vec{b}|$ then $\vec{a} = \vec{b}$.

3. Two vectors are defined by $\vec{a} = 4N[E]$ and $\vec{b} = 5N[090^\circ]$.

Find the sum vector $\vec{s} = \vec{a} + \vec{b}$ the difference vector $\vec{d} = \vec{a} - \vec{b}$.

4. Two vectors are defined by $\vec{a} = 2km[W]$ and $\vec{b} = 4km[S]$.

Find the sum vector $\vec{s} = \vec{a} + \vec{b}$ the difference vector $\vec{d} = \vec{a} - \vec{b}$.

5. Two vectors are defined by $\vec{a} = 20m[E]$ and $\vec{b} = 30m[150^\circ]$.

Find the sum vector $\vec{s} = \vec{a} + \vec{b}$ the difference vector $\vec{d} = \vec{a} - \vec{b}$.

6. Given $\vec{a} = 2\vec{i} - 3\vec{j} + \vec{k}$, $\vec{b} = -\vec{i} + \vec{j} + 2\vec{k}$, simplify the following expressions:

- $\vec{a} + \vec{b}$
- $\vec{a} - 2\vec{b}$
- $2\vec{a} - 3\vec{b}$

7. Find a unit vector parallel to the sum between $\vec{a} = 2m[E]$ and $\vec{b} = 3m[N]$.

8. Given $\vec{u} = 8m[W]$ and $\vec{v} = 10m[S30^\circ W]$, determine the magnitude and the direction of the vector $2\vec{u} - 3\vec{v}$.

9. Adam can swim at the rate of 2km/h in still water. At what angle to the bank of a river must he head if he wants to swim directly across the river and the current in the river moves at the rate of 1km/h ?

10. A plane is heading due north with an air speed of 400km/h when it is blown off course by a wind of 100km/h from the northeast. Determine the resultant ground velocity of the airplane (magnitude and direction).

11. A car is travelling at $\vec{v}_{car} = 100\text{km/h}[E]$, a motorcycle is travelling at $\vec{v}_{moto} = 80\text{km/h}[W]$, a truck is travelling at $\vec{v}_{truck} = 120\text{km/h}[N]$ and an SUV is travelling at $\vec{v}_{SUV} = 100\text{km/h}[SW]$. Find the relative velocity of the car relative to:

- motorcycle
- truck
- SUV

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	<p>1. Find the algebraic vector \vec{AB} in ordered triplet notation and unit vector notation where $A(2,-3,4)$ and $B(0,-2,3)$.</p> <p>2. Find the magnitude of the vector $\vec{v} = -2\vec{i} + \vec{j} - 3\vec{k}$.</p> <p>3. Given $\vec{a} = (-1,2,-3)$, $\vec{b} = 2\vec{i} - \vec{j} + \vec{k}$, and $\vec{c} = \vec{i} + \vec{j}$ do the required operations:</p> <ol style="list-style-type: none"> $2\vec{a} - \vec{b} + 3\vec{c}$ $3(\vec{a} + 2\vec{b}) - 2(\vec{a} - \vec{c})$ <p>4. Given $A(1,-2,3)$, $B(-2,3,-4)$, and $C(0,1,-1)$, find the coordinates of a point $D(x,y,z)$ such that $ABCD$ is a parallelogram.</p>
	<p>5. The magnitudes of two vectors \vec{a} and \vec{b} are $\vec{a} =2$ and $\vec{b} =3$ respectively, and the angle between them is $\alpha=60^\circ$. Find the value of the dot product of these vectors.</p>
	<p>6. Find the dot product of the vectors \vec{a} and \vec{b} where $\vec{a}=(1,-2,0)$ and $\vec{b}=\vec{i}-2\vec{j}-\vec{k}$.</p> <p>7. For what values of k are the vectors $\vec{a}=(6,3,-4)$ and $\vec{b}=(3,k,-2)$</p> <ol style="list-style-type: none"> perpendicular (orthogonal)? parallel (collinear)?
	<p>8. Find the angle between the vectors \vec{a} and \vec{b} where $\vec{a}=(1,-2,-1)$ and $\vec{b}=-2\vec{j}+\vec{k}$.</p> <p>9. A triangle is defined by three points $A(0,1,2)$, $B(1,0,2)$, and $C(-1,2,0)$. Find the angles $\angle A$, $\angle B$, and $\angle C$ of this triangle.</p>
	<p>10. Given the vector $\vec{a}=(2,-3,4)$, find the scalar projection:</p> <ol style="list-style-type: none"> of \vec{a} onto the unit vector \vec{i} of \vec{a} onto the vector $\vec{i} - \vec{j}$ of \vec{a} onto the vector $\vec{b}=-\vec{i}+2\vec{j}+\vec{k}$ of the unit vector \vec{i} onto the vector \vec{a}
	<p>11. Given two vectors $\vec{a}=(0,1,-2)$ and $\vec{b}=(-1,0,3)$, find:</p> <ol style="list-style-type: none"> the vector projection of the vector \vec{a} onto the vector \vec{b} the vector projection of the vector \vec{b} onto the vector \vec{a} the vector projection of the vector \vec{a} onto the unit vector \vec{k} the vector projection of the vector \vec{i} onto the vector \vec{a}
	<p>12. The magnitudes of two vectors \vec{a} and \vec{b} are $\vec{a} =2$ and $\vec{b} =3$ respectively, and the angle between them is $\alpha=60^\circ$. Find the magnitude of the cross product of these vectors.</p>

	<p>13. For each case, find the cross product of the vectors \vec{a} and \vec{b}.</p> <p>a) $\vec{a} = (1, -2, 0)$, $\vec{b} = (0, -1, 2)$ b) $\vec{a} = -\vec{i} + 2\vec{j}$, $\vec{b} = \vec{i} - 2\vec{j} - \vec{k}$</p> <p>14. Use the cross product properties to prove the following relations:</p> <p>a) $(\vec{a} - \vec{b}) \times (\vec{a} + \vec{b}) = 2(\vec{a} \times \vec{b})$ b) $(\vec{a} \times \vec{b}) \cdot (\vec{a} \times \vec{b}) + (\vec{a} \cdot \vec{b})(\vec{a} \cdot \vec{b}) = (\vec{a} \cdot \vec{a})(\vec{b} \cdot \vec{b})$</p> <p>15. Find an unit vector perpendicular to both $\vec{a} = (0, 1, 1)$ and $\vec{b} = (1, 1, 0)$.</p>
	<p>16. Find the area of the parallelogram defined by the vectors $\vec{a} = (1, -1, 0)$ and $\vec{b} = (0, 1, 2)$.</p>
	<p>17. Find the area of the triangle defined by the vectors $\vec{a} = (1, 2, 3)$ and $\vec{b} = (3, 2, 1)$.</p>
	<p>18. Find the volume of the parallelepiped defined by the vectors $\vec{a} = (0, 1, 1)$, $\vec{b} = (0, 1, 0)$ and $\vec{c} = (1, 0, 1)$.</p>
	<p>19. Consider the following vectors: $\vec{a} = \vec{i} + \vec{j} - \vec{k}$, $\vec{b} = 3\vec{i} - 2\vec{j}$, and $\vec{c} = 3\vec{i} - 2\vec{k}$. Compute the required operations in terms of the unit vectors \vec{i}, \vec{j}, and \vec{k}.</p> <p>a) $\vec{a} + \vec{b}$ b) $\vec{a} - 2\vec{b}$ c) $\vec{a} \cdot \vec{b}$ d) $\vec{b} \times \vec{c}$ e) $(\vec{a} \times \vec{b}) \cdot \vec{c}$ f) $(\vec{a} \times \vec{b}) \times \vec{c}$ g) <i>Proj</i>(\vec{a} onto \vec{b})</p>
	<p>1. Find the equation of a 2D line which</p> <p>a) passes through the points $A(0, -2)$ and $B(-3, 1)$ b) passes through the point $A(1, -3)$ and is parallel to the vector $\vec{v} = (-2, -3)$ c) passes through the point $A(-2, 3)$ and is perpendicular to the vector $\vec{v} = (3, -4)$ d) passes through the point $A(1, 1)$ and is parallel to the line $y = -2 + 3x$ e) passes through the point $A(-2, -1)$ and is perpendicular to the line $2x - 3y + 4 = 0$</p>
	<p>2. Find the point(s) of intersection between the two given lines.</p> <p>a) $\vec{r} = (1, 2) + t(3, 1)$ and $\begin{cases} x = 2 - 3s \\ y = 1 - 2s \end{cases}$ b) $\frac{x-1}{-2} = \frac{y+2}{4}$ and $y = -2x$ c) $y = -3x + 1$ and $6x + 2y - 3 = 0$</p>

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	<p>3. Find the equation of the perpendicular line to the given line through the given point.</p> <p>a) $\vec{r} = (0,1) + t(2,1)$, $B(2,-4)$</p> <p>b) $\frac{x+1}{3} = \frac{y-2}{-2}$, $B(0,2)$</p> <p>C) $2x - 3y + 4 = 0$, $B(3,1)$</p>
	<p>4. Find the distance from the given point to the given line.</p> <p>a) $\vec{r} = (-1,-2) + t(-1,2)$, $B(0,2)$</p> <p>b) $\frac{x-3}{-2} = \frac{y+2}{3}$, $B(1,3)$</p> <p>c) $x + 2y - 3 = 0$, $B(0,0)$</p>
	<p>5. Find the vector equation of a line that:</p> <p>a) passes through the points $A(0,1,2)$ and $B(-2,3,1)$</p> <p>b) passes through the point $A(2,-1,4)$ and is perpendicular on the xy plane</p> <p>c) passes through the point $A(3,-2,1)$ and is parallel to the y-axis</p> <p>d) passes through the point $A(2,-2,3)$ and is parallel to the vector $\vec{u} = (3,-2,1)$</p> <p>e) passes through the origin O and is parallel to the vector $\vec{i} - 2\vec{j}$</p>
	<p>6. Convert the equation(s) of the line from the vector form to the parametric form or conversely:</p> <p>a) $\vec{r} = (0,1,2) + t(3,4,5)$</p> <p>b) $\begin{cases} x = -1 - 2t \\ y = 1 + 3t \\ z = 2 \end{cases}$</p>
	<p>7. Convert each form of the equation(s) of the line to the other two equivalent forms.</p> <p>a) $\vec{r} = (0,1,2) + t(1,0,3)$</p> <p>b) $\begin{cases} x = -1 - t \\ y = 2 - 3t \\ z = -4 \end{cases}$</p> <p>c) $\frac{x-1}{2} = \frac{y+2}{-1} = \frac{z+3}{-2}$</p>
	<p>8. Find the x-int, y-int, and z-int for the line $\vec{r} = (1,-2,3) + t(1,-2,4)$ if they exist.</p> <p>9. Find the xy-int, yz-int, and zx-int for the line $\vec{r} = (-2,3,4) + t(-1,1,-2)$ if they exist.</p>
	<p>10. Find if the lines are parallel or not.</p> <p>a) $\vec{r} = (1,2,3) + t(1,-2,3)$, $\vec{r} = (3,2,1) + s(-2,4,-6)$</p> <p>b) $\vec{r} = (1,2,3) + t(2,1,3)$, $\vec{r} = (3,2,1) + s(4,2,-6)$</p> <p>c) $\vec{r} = (5,0,5) + t(-3,3,-6)$, $\vec{r} = (3,2,1) + s(1,-1,2)$</p>
	<p>11. In the case the lines are parallel and distinct, find the distance between the lines.</p> <p>a) $\vec{r} = (1,2,3) + t(1,-2,3)$, $\vec{r} = (3,2,1) + s(-2,4,-6)$</p> <p>b) $\vec{r} = (1,2,3) + t(2,1,3)$, $\vec{r} = (3,2,1) + s(4,2,-6)$</p> <p>c) $\vec{r} = (5,0,5) + t(-3,3,-6)$, $\vec{r} = (3,2,1) + s(1,-1,2)$</p>

	<p>12. For each case, find the distance between the given line and the given point.</p> <p>a) $\vec{r} = (1,2,-3) + t(2,-1,-2)$, $M(3,-2,1)$</p> <p>b) $\begin{cases} x = -2 + 2t \\ y = 3 + t \\ z = 1 - 2t \end{cases}$, $E(0,2,-3)$</p> <p>c) $\frac{x-2}{3} = \frac{y-1}{2} = \frac{z}{-1}$, $B(-2,1,-3)$</p>
	<p>13. Find the point of intersection if it exists.</p> <p>a) $\vec{r} = (1,2,3) + t(1,-2,3)$, $\vec{r} = (1,1,1) + s(2,-1,0)$</p> <p>b) $\vec{r} = (1,3,5) + t(0,1,2)$, $\vec{r} = (0,2,4) + s(-1,0,1)$</p>
	<p>1. Find the vector equation of a plane</p> <p>a) passing through the point $A(-1,2,-3)$ and parallel to the vectors $\vec{u} = (-2,1,0)$ and $\vec{v} = (2,-3,-1)$</p> <p>b) passing through the points $A(2,3,2)$ and $B(2,1,5)$ and $C(3,-1,0)$</p> <p>c) passing through the origin and containing the line $\vec{r} = (1,-3,2) + t(1,1,1)$</p> <p>d) passing through the point $A(2,-1,3)$ and is parallel to the yz-plane.</p>
	<p>2. Convert the vector equation for a plane to the parametric equations or conversely.</p> <p>a) $\vec{r} = (0,-1,2) + t(1,-2,3) + s(2,-3,4)$</p> <p>b) $\begin{cases} x = 1 - 2t + 3s \\ y = t - 2s \\ z = -2 + 4t \end{cases}$</p>
	<p>3. Find the scalar equation of a plane that:</p> <p>a) passes through the point $(1,2,3)$ and is perpendicular to the y-axis</p> <p>b) passes through the point $(1,0,-1)$ and is parallel to the yz-plane</p> <p>c) passes through the origin and is perpendicular to the vector $(1,-2,4)$</p>
	<p>4. Find the intersection with the coordinate axes for the plane $\pi : -2x + 3y - 6z + 12 = 0$.</p>
	<p>5. For each case, find the distance between the given plane and the given point.</p> <p>a) $\vec{r} = (1,0,2) + t(0,1,2) + s(2,0,1)$, $B(2,3,0)$</p> <p>b) $2x - 3y + z - 6 = 0$, $R(-2,0,3)$</p>

	<p>6. Find the intersection between the given line and the given plane.</p> <p>a) $\pi : 9x + 13y - 2z = 29$, $L : \begin{cases} x = 5 + 2t \\ y = -5 - 5t \\ z = 2 + 3t \end{cases}$</p> <p>b) $\pi : 4x - y + 11z + 1 = 0$, $L : \vec{r} = (-2, 4, 1) + t(3, 1, -1)$</p>
	<p>7. Find the equation of the line of intersection for each pair of planes (if it exists).</p> <p>a) $\pi_1 : 2x - 3y + z - 1 = 0$, $\pi_2 : 4x - 6y + 2z - 2 = 0$</p> <p>b) $\pi_1 : 3x + 6y - 9z - 3 = 0$, $\pi_2 : 2x + 4y - 6z - 4 = 0$</p> <p>c) $\pi_1 : x + 2y + 3z + 1 = 0$, $\pi_2 : x + 2y + z + 2 = 0$</p>
	<p>8. Find the angle between each pair of planes.</p> <p>a) $\pi_1 : x + 2y + 3z + 1 = 0$, $\pi_2 : 3x + 2y + z + 2 = 0$</p> <p>b) $\pi_1 : x + y + z + 1 = 0$, $\pi_2 : x - y - 1 = 0$</p>
	<p>9. Solve the following system of equations. Give a geometric interpretation of the result.</p> <p>1) $\begin{cases} x - 3y - 2z = -9 \\ 2x - 5y + z = 3 \\ -3x + 6y + 2z = 8 \end{cases}$</p> <p>2) $\begin{cases} x + y + 2z = -2 \\ 3x - y + 14z = 6 \\ x + 2y = -5 \end{cases}$</p> <p>3) $\begin{cases} x - y + z + 1 = 0 \\ -2x + 2y - 2z - 2 = 0 \\ 3x - 3y + 3z + 3 = 0 \end{cases}$</p> <p>4) $\begin{cases} x + y + z - 2 = 0 \\ x - y + z - 1 = 0 \\ 2x + 2y + 2z - 3 = 0 \end{cases}$</p>